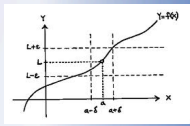
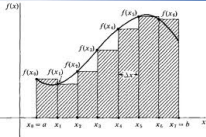


## 26 First Fundamental Thm



$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$



$$\lim_{\max \Delta x_i \rightarrow 0} \sum_{i=1}^n f(x_i) \Delta x_i = \int_a^b f(x) dx$$

$$\int_a^b f(x) dx = F(b) - F(a)$$

# The First Fundamental Theorem of Calculus

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$

### The First Fundamental Theorem of Calculus

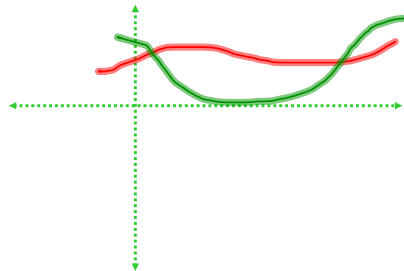
Let  $f$  be continuous on  $[a, b]$  and let  $x$  be a value in  $(a, b)$ . Then

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$

### Theorem Comparison Property

If  $f$  and  $g$  are integrable on  $[a, b]$  and if  $f(x) \leq g(x)$  for all  $x$  on  $[a, b]$ ,

$$\text{then } \int_a^b f(x) dx \leq \int_a^b g(x) dx$$



### Theorem Boundless Property

If  $f$  is integrable on  $[a, b]$  and  $m \leq f(x) \leq M$  for all  $x$  on  $[a, b]$ ,

$$\text{then } m(b-a) \leq \int_a^b f(x) dx \leq M(b-a)$$

## 26 First Fundamental Thm

### Theorem Linearity of the Definite Integral

If  $f$  and  $g$  are integrable on  $[a,b]$  and  $k$  is a real number, then

$$(i) \int_a^b kf(x)dx = k \int_a^b f(x)dx$$

and

$$(ii) \int_a^b (f(x) \pm g(x))dx = \int_a^b f(x)dx \pm \int_a^b g(x)dx$$

$$\text{EX 1} \quad \text{Suppose } \int_0^1 f(x)dx = 2 \quad \int_1^2 f(x)dx = 3$$

$$\int_0^1 g(x)dx = -1 \quad \int_0^2 g(x)dx = 4$$

$$\text{Calculate } \int_0^2 (\sqrt{3}f(t) + \sqrt{2}g(t) + \pi)dt .$$

EX 2 Find  $G'(x)$  for each of these.

$$a) G(x) = \int_3^x 4t dt$$

$$b) G(x) = \int_1^x (\cos^3(2t) \tan(t)) dt \quad -\pi/2 < x < \pi/2$$

$$c) G(x) = \int_{-2}^x (xt) dt$$

## 26 First Fundamental Thm

EX 3 Find  $\frac{d}{dx} \int_1^{x^2+x} \sqrt{2w + \sin w} dw$

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$