

**Homework 4**  
**Due Wednesday, Feb. 24th**  
Answers should be written in L<sup>A</sup>T<sub>E</sub>X.

Assume that

$$p: E \rightarrow B$$

is a covering space and  $E$  is simply connected and locally path connected. Let  $b_0 \in B$  and  $e_0 \in p^{-1}(b_0) \subset E$  be basepoints.

1. Let  $e_1 \in p^{-1}(b_0)$ . Show that there is a lift of the map of pairs

$$p: (E, e_1) \rightarrow (B, b_0).$$

That is show that there exists a map

$$p_1: (E, e_1) \rightarrow (E, e_0)$$

with  $p \circ p_1 = p$  and  $p_1(e_1) = e_0$ .

2. Show that  $p_1$  is a homeomorphism.
3. Let  $G \subset \text{homeo}(E)$  the set of all such homeomorphisms (as we let  $e_1$  vary of all points in  $p^{-1}(b_0)$ ). Show that  $G$  is a subgroup.
4. Show that the action of  $G$  on  $E$  is a deck action.
5. Show that the quotient space is homeomorphic to  $B$ .