

3.1

#25

tangent line to  
 $f(x) = 3x - 7$  at  $(3, 2)$

secant line slope

$$m_{\text{sec}} = \frac{f(x+h) - f(x)}{h} \quad \text{at } x=3, \text{ then}$$

$$\begin{aligned} m_{\text{sec}} &= \frac{f(3+h) - f(3)}{h} = \frac{3(3+h) - 7 - (3(3) - 7)}{h} \\ &= \frac{9 + 3h - 7 - 2}{h} = \frac{3h}{h} = 3 \end{aligned}$$

$\Rightarrow$  the slope is always 3 (which we already knew because it's a line)

$\Rightarrow$  slope of any tangent is also 3.

#29

$f(x) = x^3$  at  $x=2$

(tangent line slope)

+ then eqn of  
tangent line

$$m_{\text{sec}} = \frac{f(2+h) - f(2)}{h} = \frac{(2+h)^3 - 2^3}{h}$$

$$= \frac{2^3 + 3(2^2h) + 3(2h^2) + h^3 - 2^3}{h}$$

$$= \frac{12h + 6h^2 + h^3}{h} = \frac{h(12 + 6h + h^2)}{h}$$

$$= 12 + 6h + h^2 \quad \Rightarrow \quad m_{\text{tan}} = 12 + 6(0) + 0^2 = 12$$

$\Rightarrow$  tangent line:  $m = 12$  pt  $(2, 8)$   
 $f(2) = 2^3 = 8$   $\nearrow$

$$y - 8 = 12(x - 2)$$

$$y - 8 = 12x - 24$$

$$y = 12x - 16$$

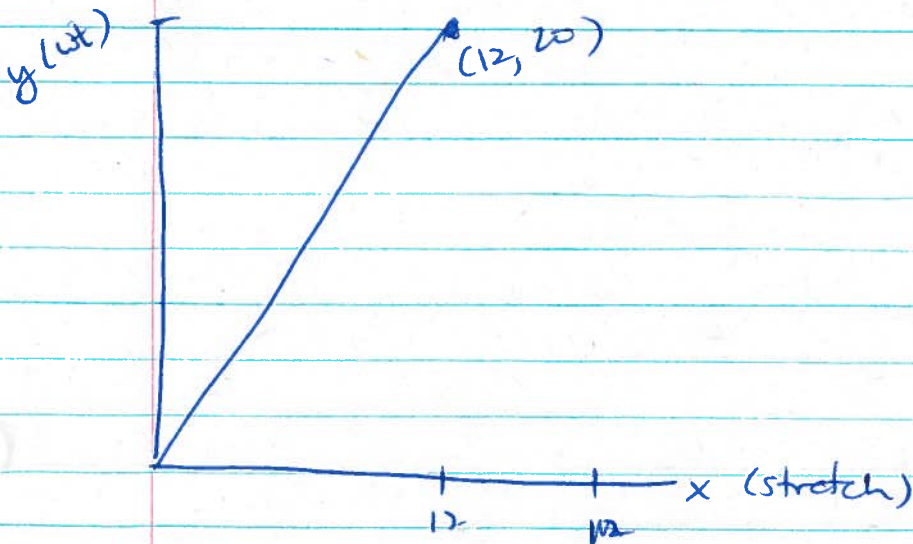
**# 41** set it up as points; we know when  
(stretch, weight)  
( $x$ ,  $y$ )

stretch =  $x = 0$  in,  $y = \text{weight} = 0$  lb  
and  $x = 6$  in,  $y = 10$  lb

$\Rightarrow$  i.e. line goes thru  $(0, 0)$  and  $(6, 10)$

$$y = \frac{5}{3}x \quad m = \frac{10}{6} = \frac{5}{3}$$

if  $x = \text{stretch} = 9.5$  in, then  $y = \frac{5}{3}(9.5) = 15.8\bar{3}$  lbs



#51 think of value as functn of time  
 $v = v(t)$  so pts are ordered pairs

$(t, v)$

We know when  $t=0$ ,  $v = \$215,000$

( $t=0$  is when it's purchased)

when  $t=10$  yrs,  $v = \$35,000$

rate of depreciation is the slope of the  
line connecting the two pts.

$(0, 215000)$   $(10, 35000)$

$$m = \frac{215000 - 35000}{0 - 10} = -18,000 \text{ (\$/yr)}$$

this means that for each additional  
year, the value decreases by \$18,000