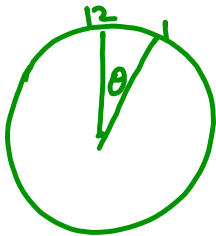
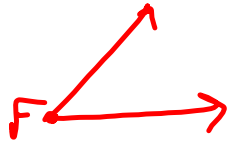

 $\angle A$ 


$$m\angle ABC \\ = m\angle CBA$$



$$\theta = \frac{360^\circ}{12} = 30^\circ$$

**Math4020 Geometry Vocabulary**

Point--> Is 0-dimensional. 

Line--> Extends forever in two directions; has no thickness; the shortest path between two points is along a line. 

Ray--> Part of a line; extends forever in only one direction and has one endpoint.



Line segment--> Shortest path between two points (straight); part of a line; has two endpoints; the intersection of two rays.



Collinear Points--> Two or more points that lie on the same line.

Angle--> Union of two rays with common endpoint called a vertex.



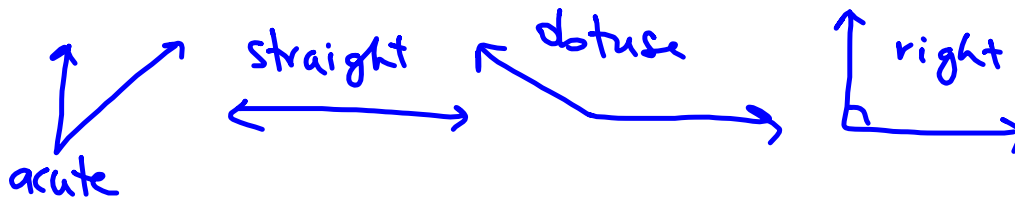
Right Angle--> A 90-degree angle; an angle that is equal in measure to an angle formed by perfectly horizontal and vertical rays.

Straight Angle--> An angle that forms a line; 180 degrees.



Acute Angle--> An angle whose measure is between 0 and 90 degrees (non-inclusive).

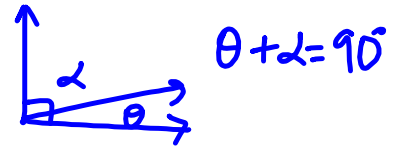
Obtuse Angle--> An angle whose measure is between 90 and 180 degrees (non-inclusive).



Perpendicular--> Two line segments are perpendicular when they meet at a right angle.

**Angle Relationships:**

Complementary Angles--> Two angles whose measures add to 90 degrees.

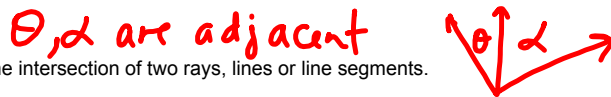


Supplementary Angles--> Two angles whose measures add to 180 degrees.

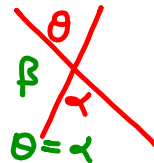


Adjacent Angles--> Angles that share a common vertex and a common side, but their interiors do not overlap.

Vertical Angles--> Two non-adjacent angles formed by the intersection of two rays, lines or line segments.



$\beta + \theta = 180^\circ$   
 $\beta + \alpha = 180^\circ$



$\theta, \alpha$  are vertical angles.

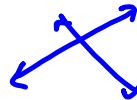
**Shapes (2-dimensional)**

Plane--> A 2-dimensional unbounded, flat region.



Coplanar points--> Two or more points that lie in the same plane.

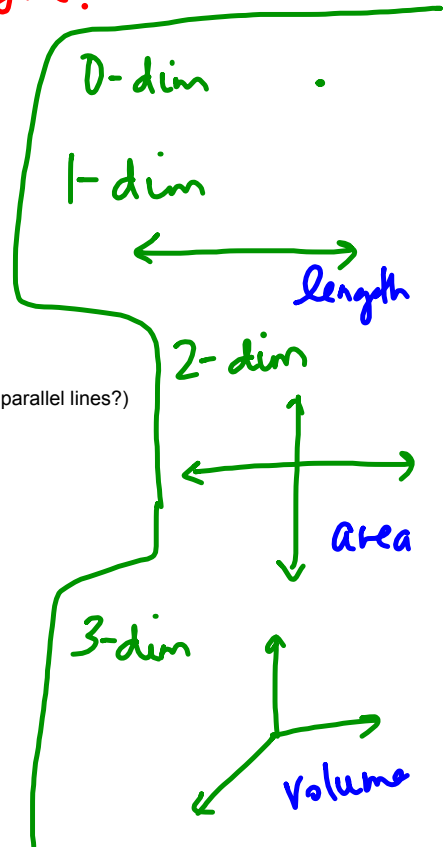
Intersecting Lines--> Two lines that intersect in only one point.



Parallel Lines--> Two distinct coplanar lines are parallel if they have no point in common.



Skew Lines--> Noncoplanar lines; lines that have no intersection. (How is this different from parallel lines?)



Congruent--> Two shapes are congruent if they are the same size and shape. That is, the first shape can be picked up and placed on top of the other.

Similar--> Two shapes are similar if they are the same shape, but not necessarily the same size; one of the shapes is a scaled version of the other.

Polygon--> A many-sided, closed 2-d shape made up of line segments for sides that meet at vertices.

Convex--> A shape is convex if every line segment, formed by connecting any two points inside the shape, is wholly contained in the shape.

Concave--> A shape is concave if it is not convex.

Regular--> A polygon is regular if all of its sides and all of its interior angles are congruent.

Interior Angle--> In a convex polygon, it's the inside angle formed by two adjacent sides.

Exterior Angle--> In a convex polygon, it's the angle formed by the side of the polygon and the extended line from the adjacent side (for every

Central Angle--> For a regular polygon, it's the angle formed by connecting a vertex to the center of the polygon and then to the consecutive vertex.

Triangle--> A 3-sided (straight sides), closed, two-dimensional shape.

Isosceles Triangle--> A triangle with at least two sides that are of equal length.

Equilateral Triangle--> A triangle with all three sides of equal length.

Scalene Triangle--> A triangle with all three sides of different length.

Obtuse Triangle--> A triangle with one obtuse angle.

Right Triangle--> A triangle with one right angle.

Acute Triangle--> A triangle with all acute angles.

Quadrilateral--> A 4-sided (straight sides), closed, two-dimensional shape.

Square--> A quadrilateral with four congruent sides and four right angles.

Rectangle--> A quadrilateral with four right angles.

Parallelogram--> A quadrilateral with two pairs of parallel sides.

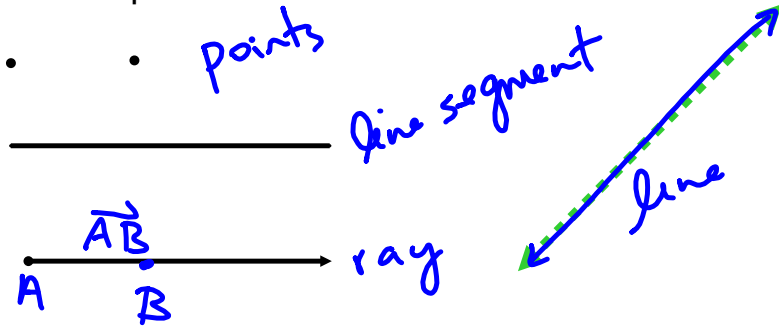
Kite--> A convex quadrilateral with two distinct pairs of adjacent congruent sides.

Rhombus--> A quadrilateral with four congruent sides.

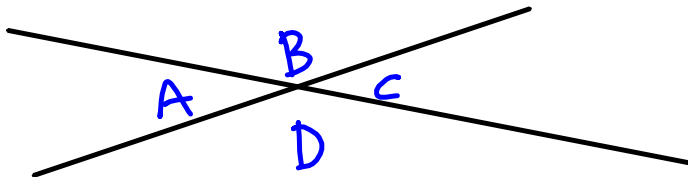
Trapezoid--> A quadrilateral with exactly one pair of parallel sides.

Isosceles Trapezoid--> A trapezoid whose non-parallel sides are congruent.

Examples:



$\vec{AB} \neq \vec{BA}$



A, C } vertical angles  
B, D }

B, C supplementary

11.1

$$\underline{A \#7} \quad 18^\circ 35' 29'' + 22^\circ 55' 41''$$

$$= 40^\circ 90' 70''$$

$$= 40^\circ 91' 10''$$

$$= 41^\circ 31' 10''$$

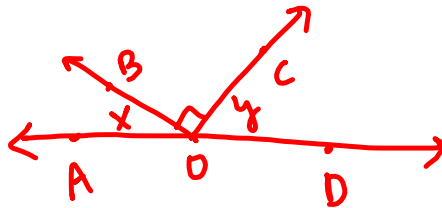
° degree  
' minute

" second

$$60 \text{ mins} = 1^\circ$$

$$60'' = 1'$$

9) (a)



$$m(\angle AOB) = \frac{1}{3} m(\angle COD)$$

$$\textcircled{1} \quad x = \frac{1}{3} y$$

$$x + 90^\circ + y = 180^\circ$$

$$\textcircled{2} \quad x + y = 90^\circ$$

$$x = \frac{1}{3} (90) \left( \frac{2}{4} \right) = \textcircled{22.5^\circ}$$

$$\textcircled{2} \quad \frac{1}{3} y + y = 90^\circ$$

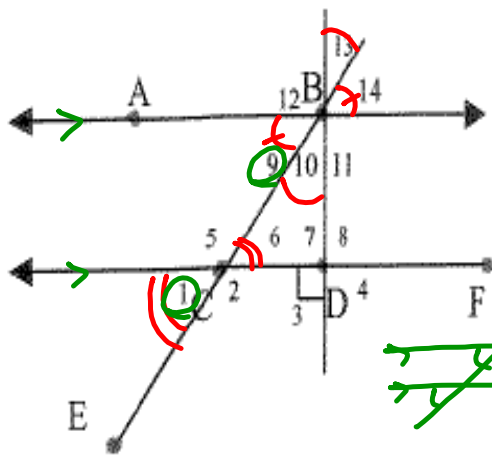
$$\frac{4}{3} y = 90^\circ$$

$$y = 90 \left( \frac{3}{4} \right) =$$

$$45 + 22\frac{1}{2}$$

$$= 67\frac{1}{2}^\circ$$

$$y = \textcircled{67.5^\circ}$$



VOCABULARY:

concurrent lines:  $\overleftrightarrow{AB}$  and  $\overleftrightarrow{CB}$   
 collinear pts: A & B or C & D  
 coplanar lines:  $\overleftrightarrow{BD}$   $\overleftrightarrow{EF}$

ANGLES:

vertical  $\angle 13 \ \& \ \angle 10$   
 corresponding  $\angle 6 \ \& \ \angle 14, \ \angle 1 \ \& \ \angle 9$   
 or  $\angle 7 \ \& \ \angle 12$   
~~alternate interior~~  
~~alternate exterior~~  
 corresponding

Z-property theorem:

