

Midterm 3 "would-be-In-class-if-there wasn't-a-holiday" Review Problems  
(No solutions provided, but you can ask about anything before the midterm)

1. Find the volume of the region that lies inside the sphere  $x^2 + y^2 + z^2 = 64$  and outside the cylinder  $x^2 + y^2 = 4$ .
2. Find the volume of the region that lies under the surface  $z = x^2 + y^2$  and above the triangle enclosed by the lines  $x=5$ ,  $y=0$ , and  $y=8x$ .
3. Evaluate  $\int_{(-1,1)}^{(5,5)} y - \frac{20}{x^2} dx + x - \frac{20}{y^2} dy$ .
4. Find the volume of the region bounded by the surface  $z = x^2 + y^2$ , the cylinder  $x^2 + y^2 = 100$  and the  $xy$ -plane.
5. Find the area of the region inside  $r = 8 \sin \theta$  and  $r = 8 \cos \theta$ .
6. Evaluate  $\int_C \frac{x+y+z}{5} ds$ , where  $C$  is the curve  $x = 3t$ ,  $y = 5 \cos(4t/5)$ ,  $z = 5 \sin(\frac{4t}{5})$ ,  $0 \leq t \leq 5\pi/4$ .
7. Find the area of the surface of the parabolic cylinder  $z = y^2$  over the triangle in the  $xy$ -plane with vertices  $(0,0)$ ,  $(0,4)$ ,  $(4,0)$ .
8. Find the volume of the region in the first octant bounded by the coordinate plane and the surface  $z = 9 - x^2 - y^2$ .
9. Write an iterated triple integral in the order  $dzdydx$  for the volume of the region enclosed by the paraboloids  $z = 50 - x^2 - y^2$  and  $z = x^2 + y^2$ .
10. Use the given transformation to evaluate the integral:  $u = x + y$ ,  $v = -2x + y$ ,  $R$  is the region bound by the lines  $y = -x + 1$ ,  $y = -x + 4$ ,  $y = 2x + 2$ ,  $y = 2x + 5$ .  $\iint_R \cos\left(\frac{y-x}{y+x}\right)$ .
11. Find the mass of a wire of density  $\delta(x, y, z) = 4z$  and has the shape of the helix  $x = 3 \cos t$ ,  $y = 3 \sin t$ ,  $z = 4t$ .